

*First Draft.*

Committee II

Pre-ICUS

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Materials

Preliminary title.

Methodological Implications and Analysis of Categorical Data  
in the Field of Social and Cognitive Development

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Table 1: Taxonomy of models for qualitative data\*

**I. Latent Attribute Models****1. Latent structure models**

Latent class model  
Latent class with response error

- Lazarsfeld & Henry (1968)
- Goodman (1974)
- Dayton & MacReady (1980)

**2. Scalability models**

Scalogram analysis  
Probabilistic scale analysis  
Multiple scale analysis  
Bi- and Multiform scales  
Probabilistic validation  
Order analysis  
Scaling of order hypothesis  
Probabilistic unfolding  
Quasi Independence model  
...

- Guttman (1950)
- Proctor (1970)
- Mokken (1971)
- Goodman (1975)
- Dayton & MacReady (1976)
- Krus et al. (1976)
- Davison (1979, 1980)
- Coombs & Smith (1973)
- Goodman (1975)

**Latent trait models**

Rasch model  
Normative ogive model  
Three parametric logistic model  
Logistic change model  
...

- Rasch (1966); Fischer (1974)
- Lord & Novick (1968)
- Birnbaum (1968)
- Fischer (1976)

**4. Factor analysis models**

FA for dichotomous variables  
Monotonicity analysis

- Muthen (1978); Christof-  
fersson (1975)
- Bentler (1970)

**II. Prediction Models****1. Dichotomous regression model**

Logit model

- Grizzle, Starmer & Koch (1969)

**2. Structural equation models**

Lisrel V  
PLS

- Jöreskog & Sörbom (1981)
- Wold (1979)

**3. Cross-classification with errors models**

Prediction analysis  
Fitting cross-classification  
Matching model

- Hildebrand et al. (1977)
- Thomas (1977)
- Hubert (1979)

**4. Multidimensional contingency table with  
Partial Least Squares (PLS)**

- Wold & Bertholet (1983)

(55)

Table 1 (continued):

III. Multinomial Response Models

1. Log-linear model - Goodman (1972); Bishop et al. (1975); Haberman (1978/79)
2. Analysis of correspondence - Benzécri (1973); Linder & Berchtold (1982)
3. Dual scaling for categorial data - Nishisato (1980)

\* Note: This taxonomy of models was initiated by Bentler (1980) and has been expanded by the present authors.

(60)

Table 6: Analysis of longitudinal samples by the Dayton & MacReady model.  
 (Table entries are probabilities for model fit)

		<u>Models</u>		
Grade:	Sample:	Guttman-structure	Model A	Model B
1	2.1	< .005	.005	.000
2	2.2	< .005	< .005	.30**
3	2.3	< .005	.23**	.25**
4	2.4	< .005	< .005	.17**

\*\* Fit

Table 7: Multiple contingency table. Cell entries are frequencies of observed pattern. This table serves as input data for the analysis with log-linear model (frequencies in brackets are set as structural zeros for quasi-independence model) and the Prediction analysis by Hildebrand et al. (1977). (Frequencies in brackets are substantive cells, the other ones are error cells)

		Phases during/after pregnancy			
		(..00)	(..10)	(..01)	(..11)
Phases before pregnancy }	(00..)	(1)	1	0	(2)
	(01..)	0	0	0	0
	(10..)	(5)	1	1	3
	(11..)	(4)	(10)	2	(15)

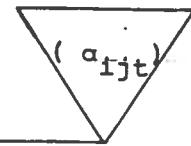
Table 8: Models and results of hypothetical structures tested for independence by log-linear models (Option: Quasi-independence model)

Model	Patterns as structural zeros	Chi <sup>2</sup>	df	p
1	0000; 1111 Concept-attainment-model)	15.99	9	.07
2	0000; 1000; 1100; 1110; 1111; (Guttman-structure)	6.02	6	.42 **
3	as model 2 but including pattern 0011	4.20	5	.52 **

\*\* substantial fit

Table 9: Taxonomy and formal integration of several scaling models (also see table 1 for comparison)

Basic-Model:

$$p(u_h) = \sum_{t=1}^s \left\{ \prod_{i=1}^n \left( \alpha_{ijt} \right) \theta_t \right\}$$


Guttman-Model:

$$\alpha_{ijt} = 0 \text{ or } 1$$

Proctor-Model:

$$\alpha_{ijt} = \beta^{x_{th}} (1 - \beta)^{n-x_{th}}$$

Dayton & MacReady-Model:

$$\alpha_{ijt} = \beta_g^{x_{th}} (1 - \beta_g)^{m_t - x_{th}} \beta_f^{y_{th}} (1 - \beta_f)^{n - m_t - y_{th}}$$

Goodman's Q.I.-Model:

$$(\alpha_{ijt}) = \left( \sum_{t=1}^s I_{ht} \theta_t + \theta_0 \prod_{i=1}^n \alpha_{ijt} \right)$$

Rasch-Model:

$$\alpha_{ijt} = \frac{\exp(\theta_i - \beta_j)}{1 + \exp(\theta_i - \beta_j)}$$

Mokken-Model:

$$\alpha_{ijt} = f_{monton}(\theta, \beta)$$

Log-Linear Model:

$$p(u_h) = u_{ij} = \gamma_{ij}^{12} \gamma_i^1 \gamma_j^2 \gamma^0 \quad (\text{for 2 by 2 tabl.})$$

$$\text{or: } \ln u_{ij} = \theta_{ij}^{12} + \theta_i^1 + \theta_j^2 + \theta^0$$

$u_h$  - the observed response pattern

$v_t$  - the expected (theoretical, "a priori") resp. pattern

$\alpha_{ijt} = p(u_h/v_t)$  - the recruitment probability

$i = 1 \dots n$  - the items

$j = 1 \dots k$  - the response alternatives

$t = 1 \dots s$  - the latent classes

$\beta_g$  - the "guessing" parameter

$\beta_f$  - the "forgetting" parameter

$m_t$  - number of zero codes in  $v_t$

$x_{th}$  - number of "1" codes in  $u_h$ , when expecting "0" in  $v_t$

$y_{th}$  - number of "0" codes in  $u_h$ , when expecting "1" in  $v_t$

$\theta$  - latent variable; subject parameter in RASCH-Model

$\beta_i$  - latent itemparameter

$I_{ht}$  - indication-parameter: 1, if  $u_h = v_t$  and 0, if  $u_h \neq v_t$

Figure 1 a/b: Examples of a "uniform-" and "biform-scale".

(a)

Item :

1 2 3 4

(1 1 1 1)

(1 1 1 0)

(1 1 0 0)

(1 0 0 0)

(0 0 0 0)

(b)

Item :

1 2 3 4

(1 1 1 1)

(1 1 0 1)

(1 0 0 1)

(0 0 0 1)

(1 1 1 0)

(1 1 0 0)

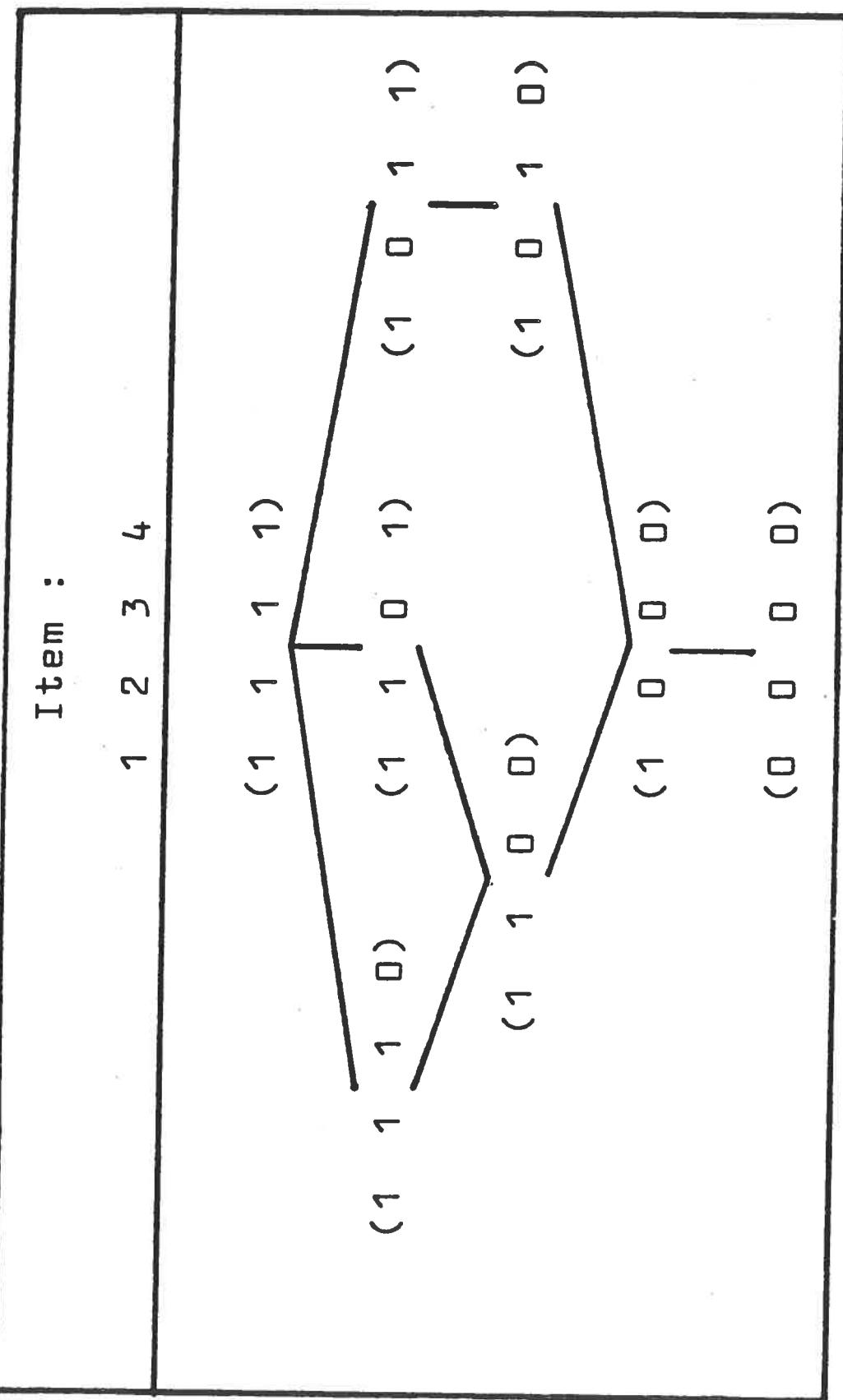
(1 0 0 0)

(0 0 0 0)

(65.8)

Figure 1 c/d: Examples of "multiform-scales".

(c)

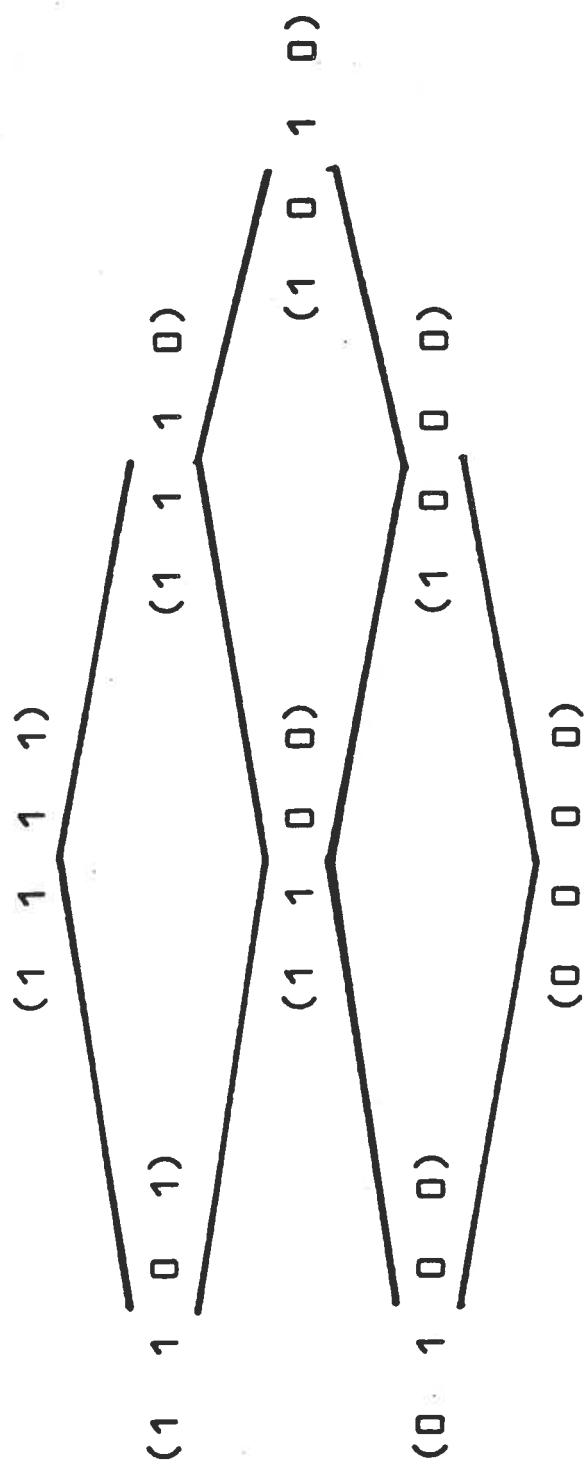


661  
q

(d)

Item :

1 2 3 4



(68)  
11

Figure 1e: Example of a symmetric diamond structure (see Shye, 1978, p. 274)

Figure 1e: Example of a symmetric diamond structure (see Shye, 1978, 274)

(2)

## Item:

Joint  
Direction

四  
三  
二  
一

四

卷之三

0 0 1 0  
0 0 0 1

卷之三

卷之三

卷之三

卷之三

卷之三

5 6 7

Lateral Direction

1 2 3 4

Figure 2: a) Model of a "cognitive-two-way-process"

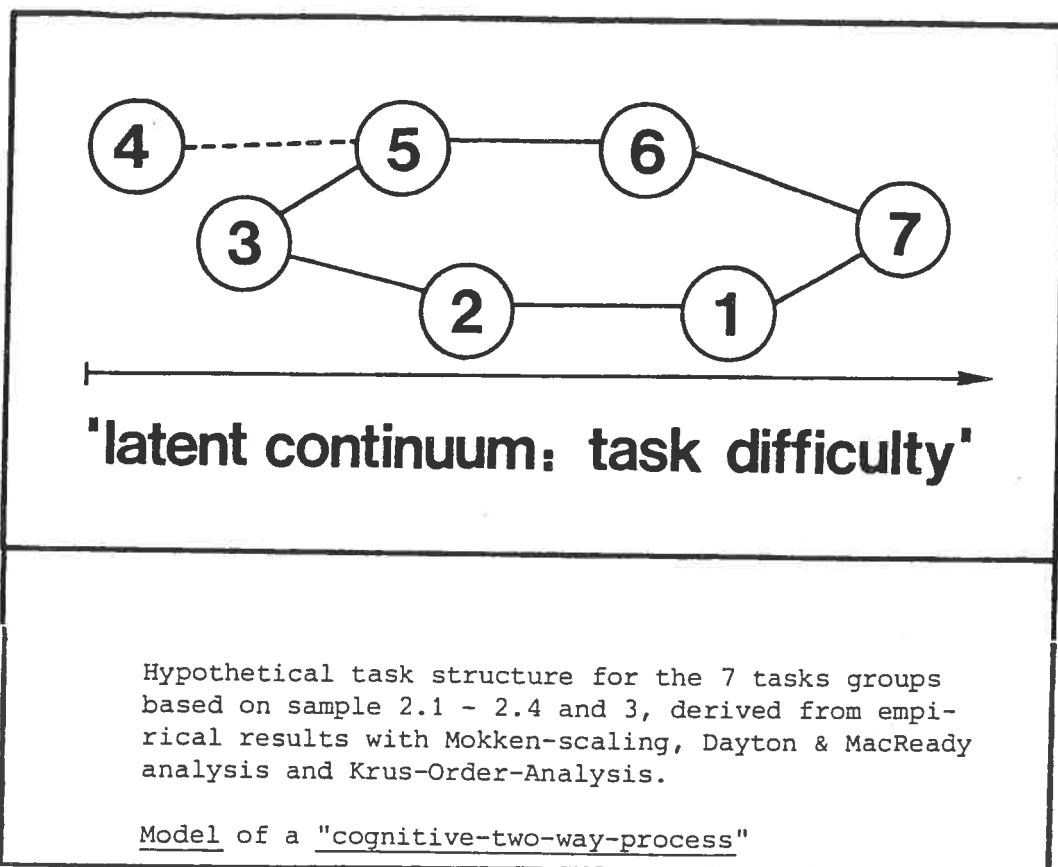


Figure 2: b) Investigated samples for invariance tasks groups

Sample 2.1: N = 45 children primary school age 5.8 - 7.1  
Sample 2.2: N = 45 " " " age 15 months later  
Sample 2.3: N = 45 " " " age 3rd grade  
Sample 2.4: N = 45 " " " age 4th grade  
Sample 3 : N = 34 children "Montessori-school" 3rd grade  
Sample 4 : N = 203 (116+87) children age 4-7 (Table 3)

Figure 2: c) Analyzed model structures for sample 4 (N = 203)

(2c)

**Analyzed models for sample 4 (N = 203)****Item: 3 2 1 5 6**

**Concept- Attainment  
Model**                    0 0 0 0 0  
                          1 1 1 1 1

**Guttman-Structure**                    0 0 0 0 0  
                          1 0 0 0 0  
                          1 1 0 0 0  
                          1 1 1 0 0  
                          1 1 1 1 0  
                          1 1 1 1 1

**Reduced-Two-Way-Biform-  
Model**                    0 0 0 0 0  
                          1 0 0 0 0  
                          1 1 0 0 0  
                          1 1 1 0 0  
                          1 0 0 1 0  
                          1 0 0 1 1  
                          1 1 1 1 1

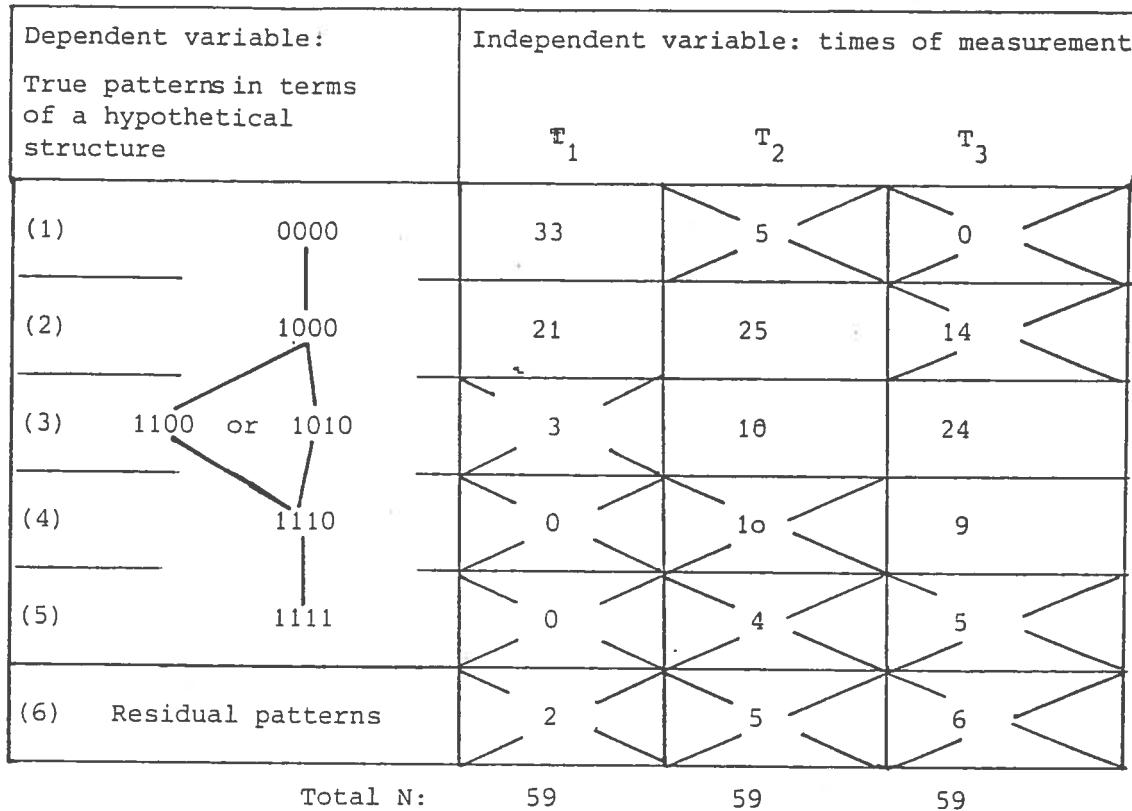
**Diamond-Structure  
Model**                    0 0 0 0 0  
                          1 0 0 0 0  
                          0 1 0 0 0  
                          1 1 0 0 0  
                          0 0 1 0 0  
                          0 1 1 0 0  
                          1 1 1 0 0  
                          0 0 0 1 0  
                          0 0 1 1 0  
                          0 1 1 1 0  
                          1 1 1 1 0  
                          0 0 0 0 1  
                          0 0 0 1 1  
                          0 0 1 1 1  
                          0 1 1 1 1  
                          1 1 1 1 1

Figure 2: d) Analyzed model structures for longitudinal sample (N = 45)

(2d)

Analyzed models for longitudinal samples 2.1 to 2.4 (N = 45)						
No. of possible patterns: 64						
No. of observed patterns: 12						
Item: 1 2 3 5 6 7						
Guttman-Structure	0 0 0 0 0 0 0 0 1 0 0 0 0 0 1 1 0 0 0 1 1 1 0 0 0 1 1 1 1 0 1 1 1 1 1 1					
Biform-Structure	Biform-Structure with patterns ommitting task 3					
Item: 1 2 3 5 6 7	Item: 1 2 3 5 6 7					
0 0 0 0 0 0 0 0 1 0 0 0 0 1 1 0 0 0 1 1 1 0 0 0 1 1 1 0 0 1 0 0 1 1 0 0 0 0 1 1 1 1 1 1 1 1 1 1	0 0 0 0 0 0 0 0 1 0 0 0 0 1 1 0 0 0 1 1 1 0 0 0 1 1 1 0 0 1 0 0 1 1 0 0 0 0 1 1 1 1 1 1 1 1 1 1 0 1 0 1 1 1 1 1 0 1 1 1					

Figure 3: Design for "aggregated group development"



DEL = -0.02 Variance-DEL = 0.00176

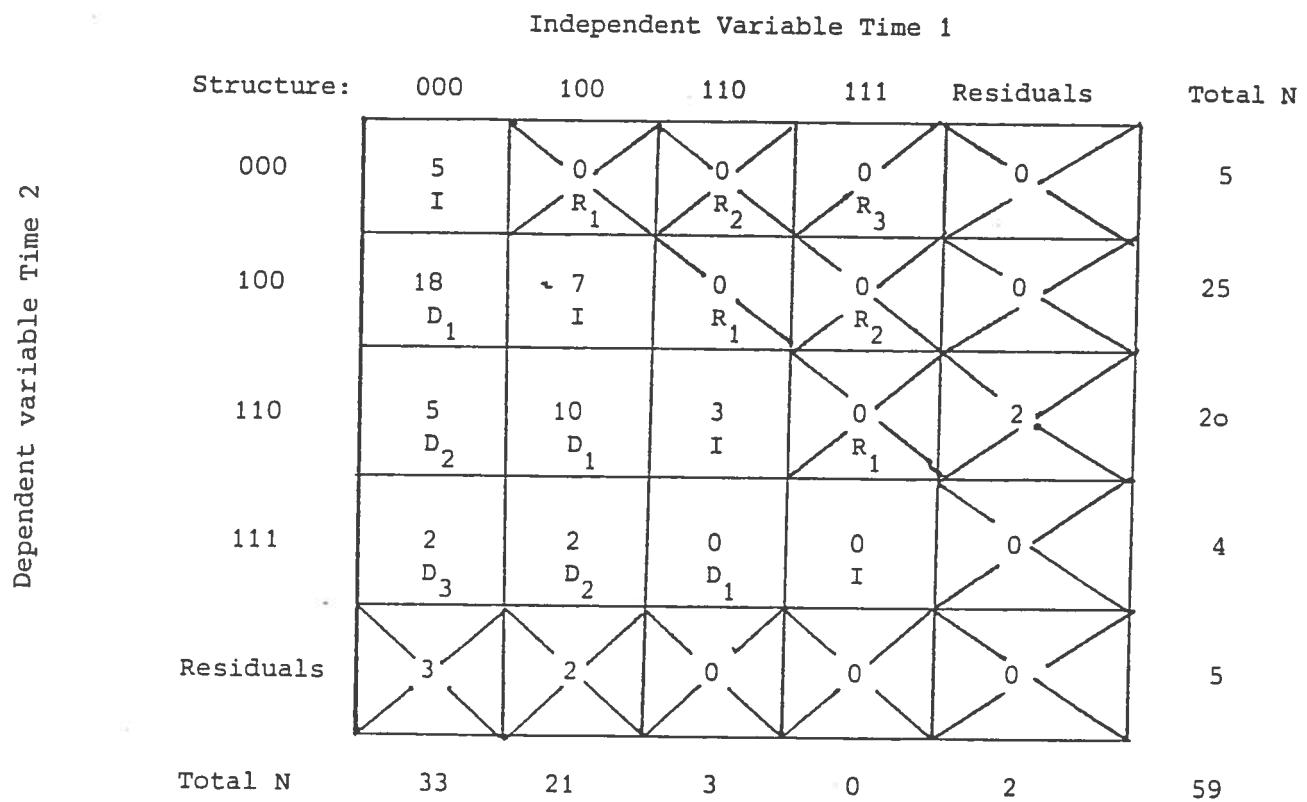
N = 176

Z = -0.52 p = 0.698

Rule Unknown = 0.656

Rule Known = 0.670

Figure 4: Design assessing "individual development"



DEL = 0.31

Variance-DEL = 0.0154

I: Identity

N = 59

$R_i$ : stage of regression

Z = 2.49 p = .006

$D_i$ : stage of development

Rule Unknown = 0.172

Rule Known = 0.119

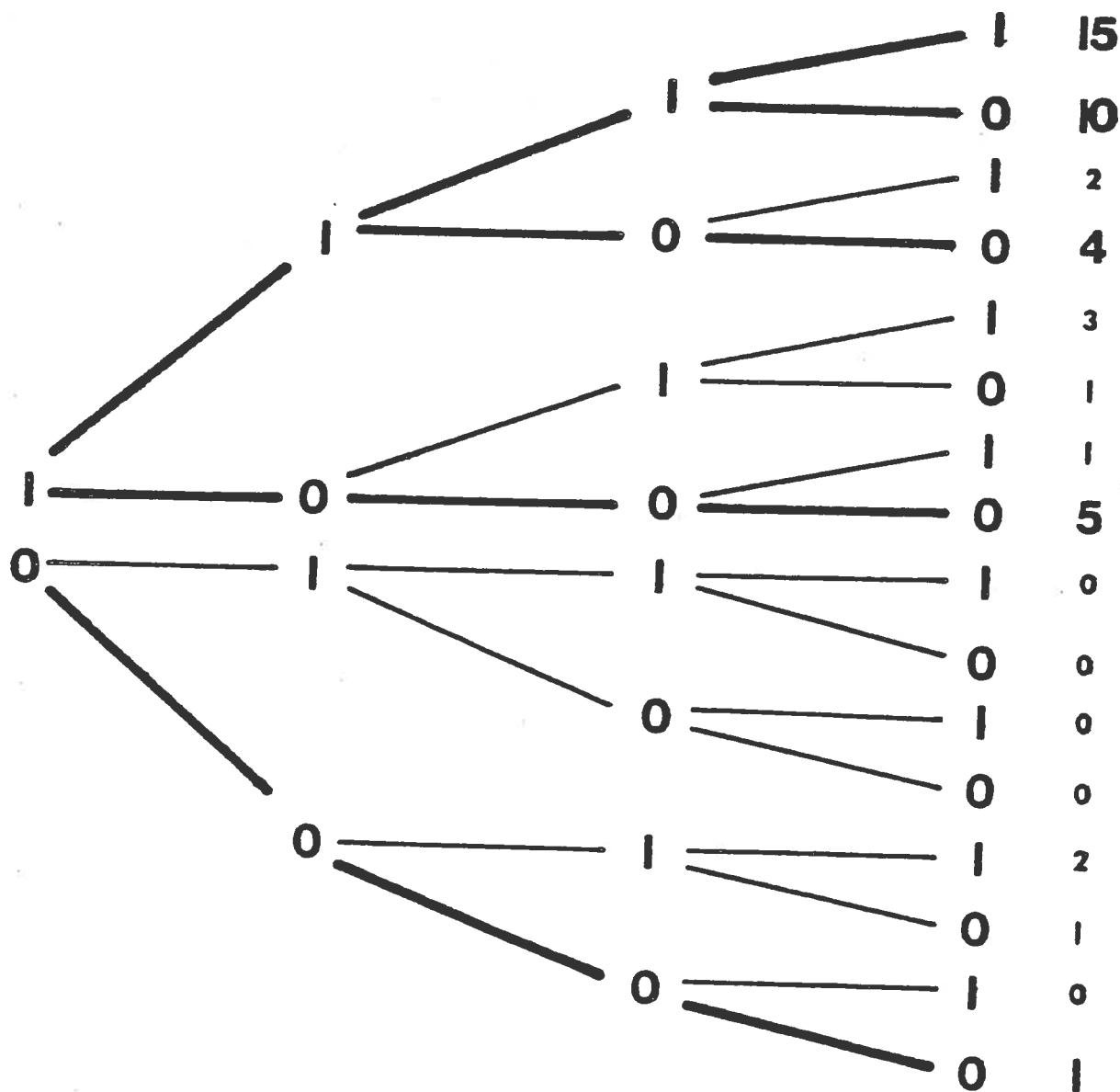


Figure 8: Sources and traditions of scaling and latent structure models

